

# A Big Data Collaborative Learning Approach for Health Risk Prediction Systems

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**ABSTRACT** - Chronic health risks have risen among young individuals due to several factors such as sedentary lifestyle, poor eating habits, sleep irregularities, environmental pollution, workplace stress etc. The problem seems to be more menacing in the near future. One possible solution is thus to design health risk prediction systems which can evaluate some critical features of parameters of the individual and then be able to predict possible health risks. As the data shows large divergences in nature with non-correlated patterns, hence choice of machine learning based methods becomes inevitable to design systems which can analyze the critical factors or features of the data and predict possible risks. This paper presents an ensemble approach for health risk prediction based on the steepest descent algorithm and decision trees. It is observed that the proposed work attains a classification accuracy of 93.72% which is comparatively higher than baseline techniques.

## General Terms

Automated Health Risk Assessment, Machine Learning, Ensemble Learning.

## Keywords

Health Risk Prediction, Ensemble Classifier, Classification Error, Accuracy.

## 1. INTRODUCTION

With increase in the sedentary lifestyle of people around the globe, different health risks are affecting people worldwide. While life expectancy has increased, but increasing health risks can be seen throughout the world [1]. The majority of the population are pre-occupied in sedentary and non-active vocations neglecting the health markers which has seen an earlier precedence of health risks in people. The major reasons happen to be [2]-[3]:

- 1) Sedentary Lifestyle
- 2) Lack of Physical Exercise.
- 3) Poor Food Choices.
- 4) Environmental Pollution.
- 5) Climate Change
- 6) Stress in everyday life etc.

Hence, an urgent need to address the health risks has become imperative. However, the cost of healthcare medications is also continuing to rise. It is the government's job to have an efficient, cost-effective medical system [4].

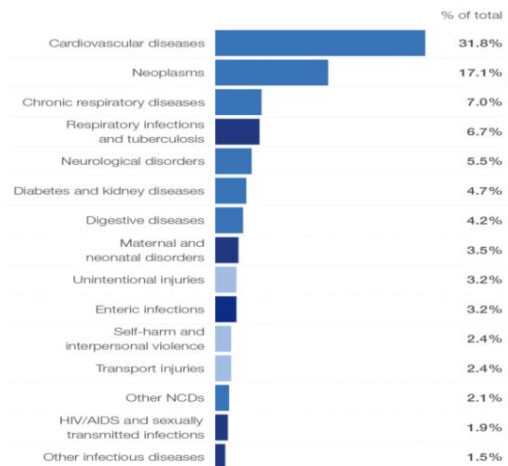


Fig 1: Global Health Risk Analysis: 2019

(Source: World Economic Forum, [1])

By presenting patient-centered medications, this can be accomplished [5]. By implementing predictive analytics in reality, further expenses spent on medical systems can be prevented. It helps to eliminate huge amounts of money wasted on unnecessary medicine and health treatments by making proper use of the significant amount of complex data produced by medical systems [6]. Health activity (diet, exercise and sleep) is generally recognized as having a significant effect on the state of human health. Such relationships between health activity and predictor of health condition (blood pressure (BP) and glucose level) are commonly researched in inpatient configurations through clinical studies [7]-[8].

## 2. NEED FOR AUTOMATED HEALTH RISK ASSESSMENT

Machine learning has been commonly used in numerous healthcare systems, such as medical imaging risk identification, diagnosis of illness, and prediction of health status from electronic health records [9]. Machine learning offers a way to automatically identify trends and predict results. There are several current experiments on various types of electronic medical data on data mining and data analytics [10]. To assess the performance of the implemented algorithm various machine learning algorithms such as Decision Tree, Support Vector Machine (SVM), and Naive Bayes are utilized. The desired outcome is based on the most frequently used metrics: accuracy, accuracy, recall, micro-average F1, macro-average F1 [11]-[12].

The medical system's digitization has led to a massive amount of medical data. These data help medical care institutions to improve the efficiency of the health system, enhance the quality of healthcare and minimize healthcare costs [9]. Big data helps businesses make better decisions to produce high revenues, improve performance, and gain comparative advantages. According to the enormous value derived from big data, the creation of Big Data systems has been actively encouraged in recent years [10]. Multiple companies from various areas have been increasingly digitized, obtaining knowledge and information from enormous quantities of big data. With the development of Healthcare Information Systems (HIS), Electronic Medical Records (EMRs), and mobile and smart phones, Healthcare has also undergone this technological transition [12]. Big Data applications have the ability to shift the enterprise to provide effective, reliable care. It can promote decision-making, aid initial infection diagnosis, and anticipate disease course. In addition, big data can assist healthcare facilities in management, price-effectiveness, and analysis customization. By giving recommendations, big data could minimize medical resources [3]-[14]. Following are the major issues for health recommendation system.

- In general, Recommendation System (RS) depends on asset popularity and can often be deceptive in HRS
- A large amount of medical content, such as text file, audio speech, and email messages, can contain unstructured data. Usually, unorganized content includes a personal touch to properly read record and analyze.
- Medical records are usually extremely complicated and ethnically diverse. The main difficulty of evaluating large-scale medical data is to create a suitable range of features from a variety of complex features without person intervention.
- Data analysis is a customer modeling problem that causes racial, gender and sexual-oriented ethical concerns.
- Generally, medical data is distributed or sparse. Data might have huge amounts of missing values owing to different human considerations [15].

### 3. EXISTING METHODS

Off late machine learning based classifiers are being used for the classification problems. Machine learning based classifiers are typically much more accurate and faster compared to the conventional classifiers. They render more robustness to the system as they are adaptive and can change their characteristics based on the updates in the dataset. The common classifiers which have been used for the classification of glaucoma cases are [16]:

Regression Models: In this approach, the relationship between the independent and dependent variable is found utilizing the values of the independent and dependent variables. The most common type of regression model can be thought of as the linear regression model which is mathematically expressed as [17]:

$$y = \theta_1 + \theta_2 x \tag{1}$$

Here,  
x represents the state vector of input variables  
y represents the state vector of output variable or variables.

$\theta_1$  and  $\theta_2$  are the co-efficients which try to fit the regression learning models output vector to the input vector [18]. Often when the data vector has large number of features with complex dependencies, linear regression models fail to fit the input and output mapping. In such cases, non-linear regression models, often termed as polynomial regression is used. Mathematically, a non-linear or higher order polynomial regression models is described as [19]:

$$y = \theta_0 + \theta_1 x^3 + \theta_2 x^2 + \theta_3 x \tag{2}$$

Here,  
x is the independent variable  
y is the dependent variable  
 $\theta_1, \theta_2, \dots, \theta_n$  are the co-efficients of the regression model. Typically, as the number of features keep increasing, higher order regression models tend to fit the inputs and targets better. A typical example is depicted in figure 2.

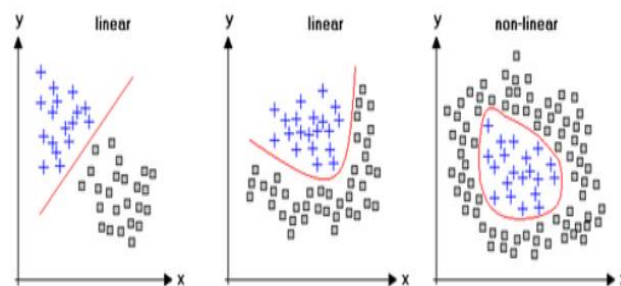


Fig 2: Linear and Non-Linear Regression fitting.

Support Vector Machine (SVM): This technique works on the principle of the hyper-plane which tries to separate the data in terms of 'n' dimensions where the order of the hyperplane is (n-1). Mathematically, if the data points or the data vector 'X' is m dimensional and there is a possibility to split the data into categories based on 'n' features, then a hyperplane of the order 'n-1' is employed as the separating plane [20]. The name plane is a misnomer since planes corresponds to 2 dimensions only but in this case the hyper-plane can be of higher dimensions and is not necessarily a 2-dimensional plane. A typical illustration of the hyperplane used for SVM based classification is depicted in figure 3.

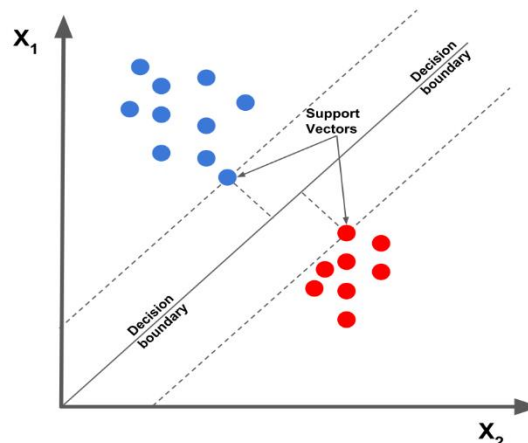


Fig 3: Separation of data classes using SVM.

The selection of the hyperplane H is done on the basis of the maximum value or separation in the Euclidean distance d given by:

$$d = \sqrt{x_1^2 + \dots + x_n^2} \tag{3}$$

Here,  
x represents the separation of a sample space variables or features of the data vector,  
n is the total number of such variables  
d is the Euclidean distance

The (n-1) dimensional hyperplane classifies the data into categories based on the maximum separation. For a classification into one of 'm' categories, the hyperplane lies at the maximum separation of the data vector 'X'. The categorization of a new sample 'z' is done based on the inequality:

$$d_x^z = \text{Min}(d_{c1}^z, d_{c2}^z \dots d_{c2=m}^z) \tag{4}$$

Here,  
 $d_x^z$  is the minimum separation of a new data sample from 'm' separate categories  
 $d_{c1}^z, d_{c2}^z \dots d_{c2=m}^z$  are the Euclidean distances of the new data sample 'z' from m separate data categories.

Neural Networks: Owing to the need of non-linearity in the separation of data classes, one of the most powerful classifiers which have become popular is the artificial neural network (ANN). The neural networks are capable to implement non-linear classification along with steep learning rates. The neural network tries to emulate the human brain's functioning based on the fact that it can process parallel data streams and can learn and adapt as the data changes [21]. This is done through the updates in the weights and activation functions. The mathematical model of the neural network is depicted in figure 4.

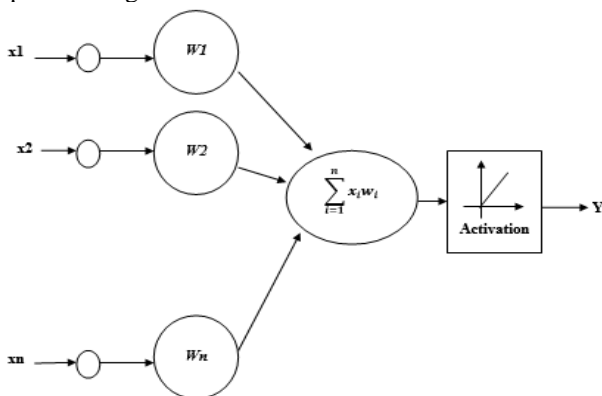


Fig 4: Mathematical Model of Single Neuron.

The mathematical equivalent of an artificial neuron is depicted in figure 4 where the output can be given by:

$$y = f(\sum_{i=1}^n x_i w_i + b) \tag{5}$$

Here,  
x denote the parallel inputs  
y represents the output  
w represents the bias  
f represents the activation function

The neural network is a connection of such artificial neurons which are connected or stacked with each other as layers. The neural networks can be used for both regression and classification problems based on the type of data that is fed to them. Typically the neural networks have 3 major conceptual layers which are the input layer, hidden layer and output layer. The parallel inputs are fed to the input layer whose output is fed to the hidden layer [22]. The hidden layer is responsible for analysing the data, and the output of the hidden layer goes to the output layer. The number of hidden layers depends on the nature of the dataset and problem under consideration. If the neural network has multiple hidden layers, then such a neural network is termed as a deep neural network [23]. The training algorithm for such a deep neural network is often termed as deep learning which is a subset of machine learning. Typically, the multiple hidden layers are responsible for computation of different levels of features of the data [24].

Decision Trees: The decision trees are another class of multivariate classifiers. The tree tries to estimate event outcomes based on probabilities, where the target or output variable is dependent on several input or governing variables. The decision tree is obtained by recursively splitting the source data set (know as root node) into subsequent branches termed as the children [25].

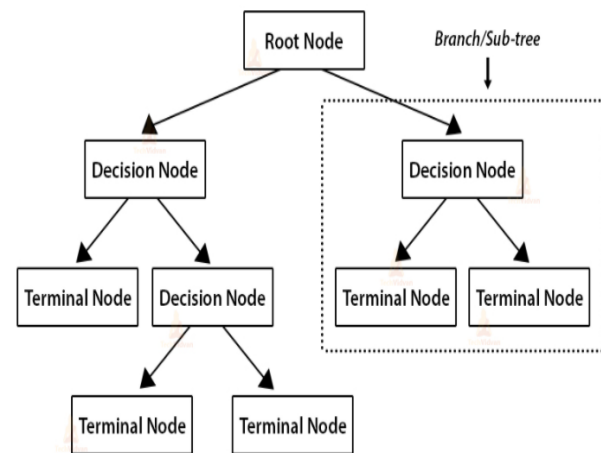


Fig 5: A Typical Decision Tree Model

The decision tree structure is depicted in figure 5 which exhibits the recursive classification method.

#### 4. PROPOSED METHODOLOGY

The proposed methodology presents an ensemble of the neural networks and decision trees to extract the attributes of both classifying paradigms which are:

- 1) Pattern recognition
- 2) Probabilistic Classification

The pattern recognition is performed using the gradient decent or scaled conjugate gradient. To update  $\theta_1$  and  $\theta_2$  values in order to reduce Cost function (minimizing MSE value) and achieving the best fit line the model uses Gradient Descent. The idea is to start with random  $\theta_1$  and  $\theta_2$  values

and then iteratively updating the values, reaching minimum cost. The main aim is to minimize the cost function J [26].

If the descent vector is given by 'g', then  

$$g = f(J, w) \tag{6}$$

Here,  
 F stands for a function of.  
 W are the network weights

The gradient descent based approach is often employed to train a neural model such that, the increase in iterations continuously decrease a cost function defined in the above section. Moreover, as discussed in the previous approaches, there are several techniques and mechanisms to train a neural network out of which one of the most effective techniques is the back propagation based approach. The scaled conjugate gradient tries to find the steepest descent vector prior to weight update in each iteration and is mathematically given by [27]:

$$A_0 = -g_0 \tag{7}$$

Here,  
 A is the initial search vector for steepest gradient search  
 g is the actual gradient

$$w_{k+1} = w_k + \mu_k g_k \tag{8}$$

Here,  
 $w_{k+1}$  is the weight of the next iteration  
 $w_k$  is the weight of the present iteration  
 $\mu_k$  is the combination co-efficient

For any iteration k, the search vector is given by:

$$A_k = -g_k + \beta_k A_{k-1} \tag{9}$$

And

$$\beta_k = \frac{(|g_{k+1}|^2 - g_{k+1}^T g_k)}{g_k^T g_k} \tag{10}$$

Here,  
 The customary g represents  $\frac{\partial e}{\partial w}$

The ensemble also uses the decision trees which is effective for multi-class decisions. For a multi-class classification, the conditional probability of the sentiment can be also seen as an overlapping event with the classification occurring with the class with maximum conditional probability [29]. The probability of inaccurate classifications based on the Gini's Index is given by [28]:

$$G = Prob(C) * [1 - Prob(C)] \tag{11}$$

Here,  
 G denotes the Gini's Index.  
 Prob(C) denotes probability of a data sample to belong to class 'C'.  
 1 - Prob(C) denotes the complement of probability of a data sample to belong to class 'C'.

The continued or recursive splitting generates binary trees at every decision node and the final Gini Index is computed as the weighted sum of all the individual splits. Thus the total split index is given by:

$$G_{tot} = \sum_{i=1}^k G_{L,i} w_i + G_{R,i} w_i \tag{12}$$

Here,  
 $G_{tot}$  denotes total Gini Index  
 $G_{L,i}$  denotes Left Partitioned Tree's Index

$G_{R,i}$  denotes Right Partitioned Tree's Index  
 $w_i$  denotes the weights of the partitioning.

The performance metrics of the classifiers are generally computed based on the true positive (TP), true negative (TN), false positive (FP) and false negative (FN) values which are used to compute the accuracy and sensitivity of the classifier, mathematically expressed as [30]:

$$Ac = \frac{TP+TN}{TP+TN+FP+FN} \tag{13}$$

Sensitivity: It is mathematically defined as:

$$Se = \frac{TP}{TP+FN} \tag{14}$$

$$Recall = \frac{TP}{TP+FN} \tag{15}$$

$$Precision = \frac{TP}{TP+FP} \tag{16}$$

$$F - Measure = \frac{2.Precision.Recall}{Precision+Recall} \tag{17}$$

The aim of any designed approach is to attain high values of accuracy of classification along with other associated parameters. The computation complexity of the system often evaluated in terms of the number of training iterations and execution time is also a critically important metric which decides the practical utility of any algorithm on hardware constrained devices.

### 5. EXPERIMENTAL RESULTS

The system has been designed on MATAB 2020a. The results obtained are presented subsequently.

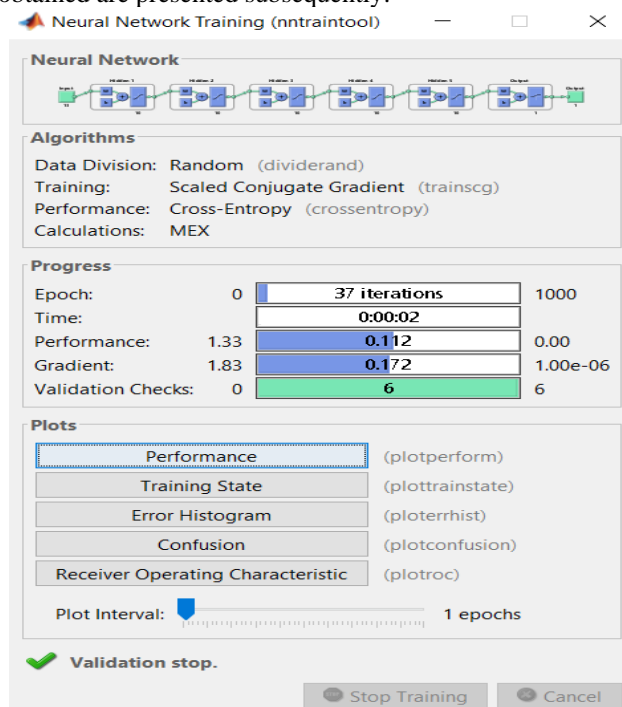


Fig 6: The Regression Analysis Model

Figure 6 depicts the regression analysis model



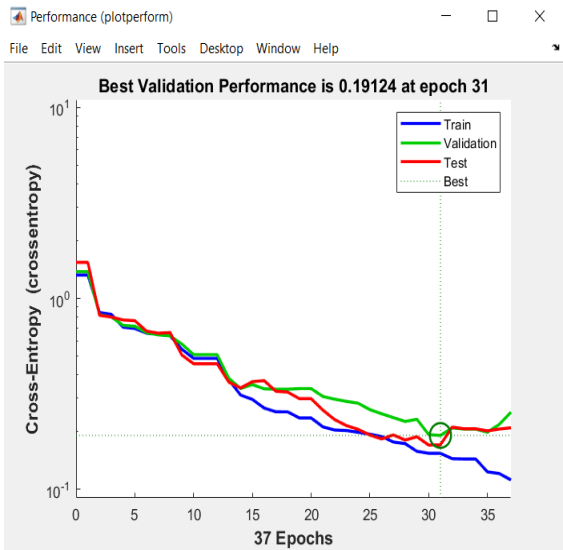


Fig 7: Variation of MSE

Figure 7 shows the variation of the cost function (MSE) in this case with the increase in the number of iterations (epochs). The training stops for regression analysis in 2 cases:

- 1) Objective function stabilizes for validation check counts.
- 2) Maximum epochs are over.

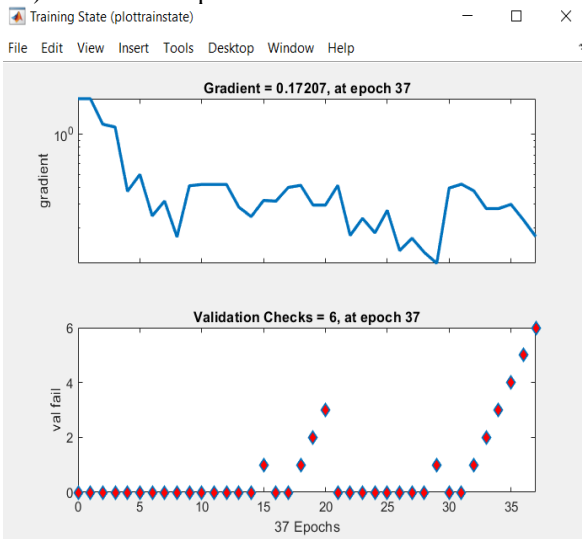


Fig 8: Training States

Figure 8 depicts the variation of the training states as a function of iterations.

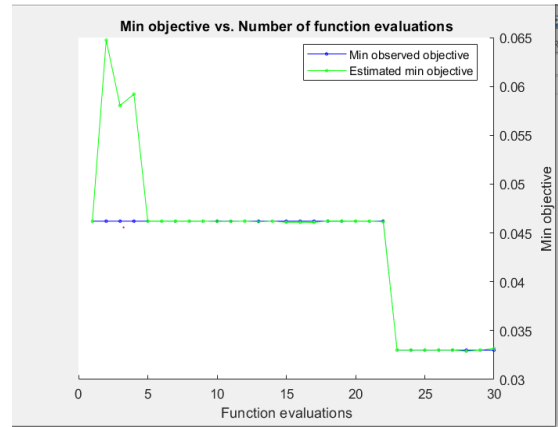


Fig 9: Function Evaluations.

The ensemble tree using which the iterations to convergence are achieved are depicted in figure 9. The iterations to convergence and the learning rate are depicted subsequently.

Iter	Eval	Objective	Objective runtime	BestSoFar (observed)	BestSoFar (estim.)	Method	NumLearningCycles
6	Accept	0.069307	0.45767	0.046205	0.046209	LogitBoost	14
7	Accept	0.12211	0.5917	0.046205	0.046209	Bag	14
8	Accept	0.069307	0.3568	0.046205	0.046209	AdaBoostM1	14
9	Accept	0.17922	0.81442	0.046205	0.046209	AdaBoostM1	36
10	Accept	0.046205	1.3957	0.046205	0.046174	GentleBoost	49
11	Accept	0.052805	0.49898	0.046205	0.046181	GentleBoost	27
12	Accept	0.079208	9.5903	0.046205	0.046208	AdaBoostM1	461
13	Accept	0.059406	7.6097	0.046205	0.046145	GentleBoost	293
14	Accept	0.049505	1.8147	0.046205	0.046204	GentleBoost	77
15	Accept	0.059406	5.8468	0.046205	0.04609	GentleBoost	252
16	Accept	0.069307	0.29398	0.046205	0.046088	GentleBoost	10
17	Accept	0.059406	11.485	0.046205	0.046081	GentleBoost	496
18	Accept	0.58746	10.209	0.046205	0.046221	RUSBoost	456
19	Accept	0.072607	1.6996	0.046205	0.04622	LogitBoost	71
20	Accept	0.049505	0.75167	0.046205	0.046209	GentleBoost	30
21	Accept	0.09571	3.1963	0.046205	0.046209	RUSBoost	146
22	Accept	0.082508	1.6661	0.046205	0.046145	AdaBoostM1	82
23	Best	0.033003	2.9963	0.033003	0.033016	LogitBoost	120
24	Accept	0.052805	3.8106	0.033003	0.033016	GentleBoost	149
25	Accept	0.046205	2.509	0.033003	0.033019	GentleBoost	105
26	Accept	0.085809	1.2391	0.033003	0.033016	AdaBoostM1	60
27	Accept	0.082508	0.42916	0.033003	0.033018	RUSBoost	17
28	Accept	0.046205	9.94227	0.033003	0.032894	LogitBoost	38
29	Accept	0.072607	9.8994	0.033003	0.033016	AdaBoostM1	498
30	Accept	0.052805	11.3	0.033003	0.033166	LogitBoost	488

Fig 10: Iterations to Convergence

The iterations to convergence and ensemble method is depicted in figure 10. It can be seen that eh system converges in 30 iterations.

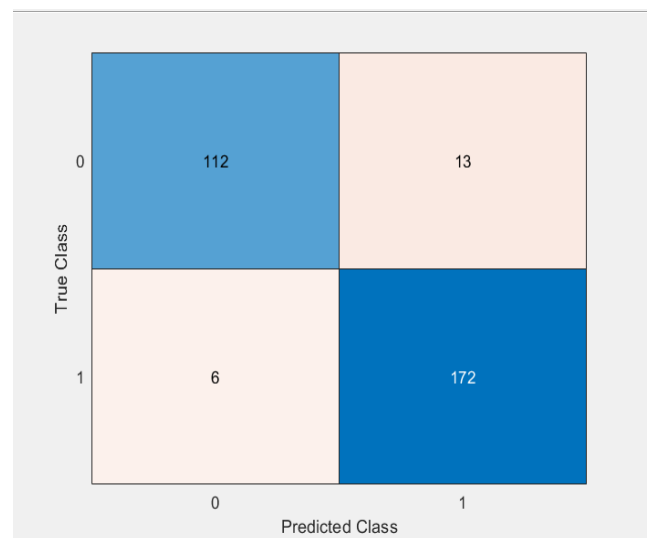


Fig 11: Confusion Matrix

The confusion matrix is depicted in figure 11. The accuracy is thus computed as:

$$Ac = \frac{172 + 112}{172 + 112 + 13 + 6} = 93.72\%$$

## 6. CONCLUSION

It can be concluded that the necessity of automated tools for health risk estimation is necessary keeping in mind the lifestyle changes risks at earlier ages. This paper presents an ensemble learning based approach for health risk estimation. In this classifier design, the training data which is labelled is applied to the algorithm for pattern analysis which assumes the data events in classes to be true. Based on the analyzed patterns, the new data sample's probability to belong to a specific category is evaluated. The performance of the system has been evaluated in terms of the true positive, true negative, false positive and false negative rates, Based on these metrics, the accuracy of the system has been evaluated. The experimental results show that the proposed system attains a classification accuracy of 93.7% which is comparatively higher than the existing system [1] which attains a classification accuracy of 87.7% for the same dataset. The number of iterations are also less which are 30 for convergence. Thus, the proposed system effectively predicts health risks based on medical record datasets which relatively high accuracy.

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