

# Effect of Process Parameters on Fracture Depth and Thickness Distribution in Single Point Incremental Forming

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**Abstract**— New methods of forming sheet metal are now at a stage where it is possible to make either custom manufactured parts or to manufacture small batch production quantities, with very short turnaround times. Current developments have been focused on forming symmetric parts using CNC technology, without the need for costly dies. Incremental forming uses the same principle that of rapid prototyping i.e. forming a model step-by-step. Single Point Incremental Sheet Forming has the potential to revolutionize sheet metal forming, making it accessible to all levels of manufacturing. In this work FEA of incremental sheet metal forming was carried out using ABAQUS/Explicit. Formability of sheet material was predicted from a tension test. Theoretical forming limit diagrams which were constructed using Levy-Mises flow rule for plastic deformation. Rotational parts i.e. frustum of cone were formed by incremental method using 3axis CNC machine. L9 model was selected using design of experiment by Taguchi method which gave 9 experimental runs to be conducted. Three process parameters considered were tool diameter, vertical step size and feed rate. Responses measured were fracture depth and thickness distribution. The most influencing parameters and there percent contribution to response is calculated using ANAOVA statistical models.

**Keywords**—Single point incremental formin, sheet metal forming, formability parameters

## I. INTRODUCTION

Sheet metal is one of the most fundamental forms used in metal working, and can be cut and bent into a variety of shapes. Modern continuous rolling mills produce large quantities of thin sheet metal at low cost. A substantial fraction of all metals are produced as thin hot or cold-rolled sheet; this is then formed in secondary processes into automobiles, domestic appliances, building products, aircraft, food cans and most of other familiar products. Sheet metals parts have the advantage that the material has a high elastic modulus and high yield strength so that the parts produced can have a good strength-to-weight ratio.

## II. FORMABILITY AND TENSILE TEST

The most commonly used test for predicting metal formability is the uniaxial tension test. Specimens were prepared and test is conducted as per the standard of ASTM standard B-557-M which is Standard Test Methods for Tension Testing Wrought and Cast Aluminum- and Magnesium-Alloy Products. Sheet metals possess anisotropy i.e. their properties are dependent of the direction. Hence to find anisotropy; tensile tests were conducted along three different directions, with the tensile axis being parallel (0), diagonal (45) and perpendicular (90) to the rolling direction of sheet. The strain hardening coefficient (n) and strength coefficient (k) of material were determined from the slope of true stress-true strain curve when plotted on logarithmic coordinates. The relation is given by following equation:

$$\sigma = k e^n \quad (1)$$

where  $\sigma$ : True stress

k: Strength coefficient

n: Strain hardening coefficient

e: Engineering strain

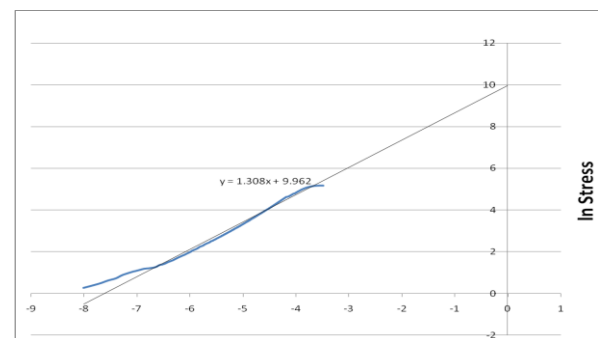


Fig 1: Log-Log Plots of True Stress and True Strain

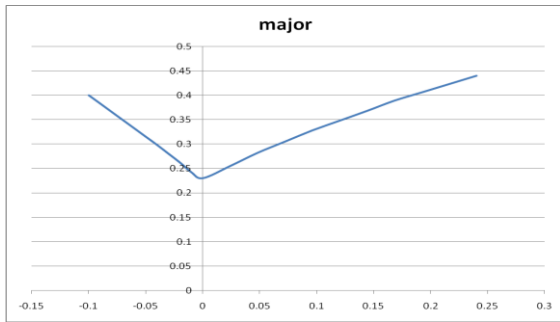


Fig. 2. Theoretical forming limit diagram

Tensile properties, strain hardening coefficient (n) and strength coefficient (k) of material for three different rolling directions are as shown in Table 1.

TABLE I. TENSILE PROPERTIES OF MATERIAL

Direction	Yield Stress MPa	UTS MPa	k MPa	n
0°	179.87	182.69	498.84	0.13
45°	158.74	167.62	402.84	0.14
90°	187.53	183.69	493.74	0.19
Average	172.40	174.86	449.57	0.15
X <sub>m</sub> = (X <sub>0</sub> +2X <sub>45</sub> +X <sub>90</sub> )/4; where X is k and n				

### III. THEORETICAL PREDICTION OF FORMING LIMIT DIAGRAM

Forming limit diagram is needed to predict the behaviour of sheet during forming and to compare the strain development in cup. Theoretical prediction of FLD is made using Levy-Mises flow rule for limiting strain. The limiting strains are calculated using Levy-Mises flow rule for plastic deformation in which  $\lambda$ ,  $e_1$  and  $e^2$  are given by:

$$\lambda = \frac{\bar{\epsilon}}{2(1+r_m)\bar{\sigma}^{m-1}} \quad (2)$$

The values of  $\sigma_1$  and  $\sigma_2$  are calculated by the yield criterion; by putting value of  $\sigma_1$  from 0 to UTS.

$$(\sigma_1 + \sigma_2)^m + (1 + 2r_m)(\sigma_1 - \sigma_2) = 2(1 + r_m)\bar{\sigma}^m \quad (3)$$

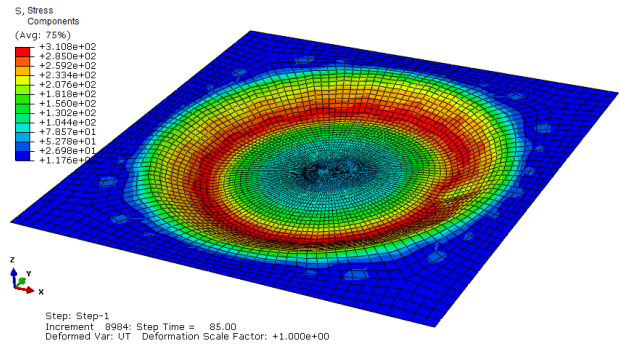


Fig. 3. Finite element analysis

Using the equations (4) and (5), the major and minor strains are calculated and with those values FLD is plotted. Major strain is fixed on Y axis and minor strain is fixed on X axis.

$$e_1 = [(1+2r_m)(\sigma_1 - \sigma_2)^{m-1} + (\sigma_1 + \sigma_2)^{m-1}] \quad (4)$$

$$e_2 = [-(1+2r_m)(\sigma_1 - \sigma_2)^{m-1} + (\sigma_1 + \sigma_2)^{m-1}] \quad (5)$$

### IV. FINITE ELEMENT ANALYSIS OF SPIF

For the finite element analysis of incremental forming; HYPERMESH was used as pre-processor and ABAQUS/Explicit is used as solver and post-processor. The tool is a special part which is defined as analytically rigid sphere as only half of its lower surface came in contact with blank. Sheet blank was defined as continuous and homogeneous shell element 2304 of thickness 0.46 mm. Figure 3.5 shows the part modeling of tool and sheet blank.

### V. DESIGN OF EXPERIMENTS AND WORK

Design of Experiments using Taguchi method is an organized method to yield the maximum desired output with the least number of experimentation and also to determine the factors that influence the output of the experiment. The main objectives of the design of experiments are to minimize the number of trials, to get simultaneous variation in all process parameters, to determine the factor that influences the output most. The experimental runs and responses are as stated in table 2.

Table 2. Experimental runs and responses

Run Id	Process Parameters			Responses	
	Tool Dia.	Step Size	Feed Rate	Final Thickness	Fracture Depth
1	8	0.5	300	0.26	35
2	8	0.62	400	0.27	24
3	8	0.75	500	0.27	18
4	10	0.5	400	0.25	35
5	10	0.62	500	0.24	27
6	10	0.75	300	0.23	16
7	12	0.5	500	0.24	35
8	12	0.62	300	0.23	27
9	12	0.75	400	0.23	19

For conducting an experiment we had a choice of three input parameters which were tool diameter, vertical step size and feed rate. So 3 Factor- 3 Level i.e. L9 model is used which gave 9 experimental runs to be conducted. It was created using MINITAB statistical package.

The basic things required to conduct an experiment are sheet metal blank, blank holder, single point forming tool, forming Machinery i.e. CNC Milling Machine. Machine used was make of Lakshmi Machine Works (Model LV45) with FANUC Oi MATE MC control system.

## VI. TAGUCHI ANALYSIS AND ANOVA OF FINAL THICKNESS

To analyse the design of an experiment; observed response of final thickness and signal to noise ratio are calculated and represented in Table 3.

Table 3. Analyse the design of an experiment

Run Id	Final Thickness (mm)	S/N Ratio	Mean of means
1	0.26	-11.7005	0.26
2	0.27	-11.3727	0.27
3	0.27	-11.3727	0.27
4	0.25	-12.0412	0.25
5	0.24	-12.3958	0.24
6	0.23	-12.7654	0.23
7	0.24	-12.3958	0.24
8	0.23	-12.7654	0.23
9	0.23	-12.7654	0.23

In order to maximize the S/N ratio, the following levels of factors were used: tool diameter– level 1(8 mm), steps size– level 1 (0.5 mm) and feed rate– level 3(500 mm/min).

Fig. 4 shows effect of individual factor on average S/N ratio of final thickness.

Examination of the calculated Fisher's values (F) for all control factors also showed high influence and low influence factors on the final thickness as shown in Table 4.3. Fishers' value was calculated for each process parameters. The optimum test conditions were estimated from the significant factors. The computed value of  $F_{cal}$  (28.0) was more than that from statistical  $F_{tab}$  (19.0). The last column of the above table

Fig. 4. Effect of individual factor on average S/N ratio

indicates the percentage of contribution (%P) of each factor, thus exhibiting the level of influence on the quality characteristics. The Table 4.3 shows tool diameter, steps size and feed rate have percentage contributions of 84.86, 9.09 and 3.04 on the final thickness of sheet blank respectively.

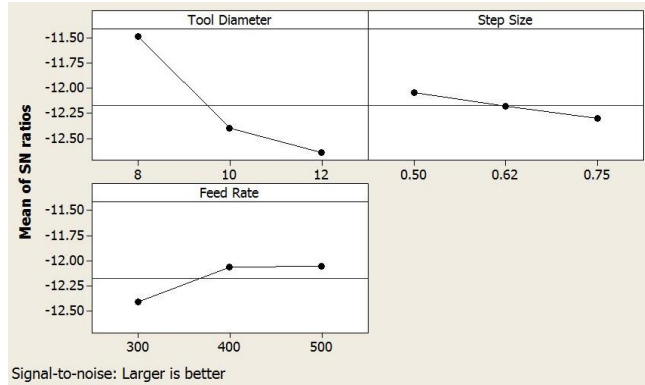


Table 4. ANOVA of final thickness

Parameter	Sum of squares	Mean squares	$F_{cal}$	$F_{tab}$	Contribution
Tool Dia.	0.001867	0.000933	28.0	19.0	84.86
Step Size	0.000200	0.000100	3.0	19.0	9.09
Feed Rate	0.000067	0.000033	1.0	19.0	3.04
Error	0.000067	0.000033			
Total	0.002200				

## VII. TAGUCHI ANALYSIS AND ANOVA OF FRACTURE DEPTH

To analyse the design of an experiment; observed response of final thickness and signal to noise ratio are calculated and represented in Table 5. The estimated individual factor's effect on mean depth for deformed section of Al alloy sheet is shown in Figure 5.

Table 5. Analyse the design of an experiment

Run Id	Fracture Depth (mm)	S/N Ratio	Mean of means
1	35	-11.7005	0.26
2	24	-11.3727	0.27
3	18	-11.3727	0.27
4	35	-12.0412	0.25
5	27	-12.3958	0.24
6	16	-12.7654	0.23
7	35	-12.3958	0.24
8	27	-12.7654	0.23
9	19	-12.7654	0.23

Examination of the calculated Fisher's values ( $F_{cal}$ ) for all control factors also showed a very high influence of step size and low influence of tool diameter and feed rate as shown in Table 4.5. F value was calculated for each design parameters. The optimum test conditions were estimated from the significant factors. The computed value of  $F_{cal}$  (65.45) was more than the statistical  $F_{tab}$  (19.00).

Parameter	Sum of squares	Mean squares	F <sub>cal</sub>	F <sub>tab</sub>	Contribution
Tool Dia.	2.889	0.000933	0.42	19.0	0.63
Step Size	450.889	0.000100	65.4	19.0	97.49
Feed Rate	0.889	0.000033	0.13	19.0	0.19
Error	6.889	0.000033			
Total	461.556				

Table 6. ANOVA of fracture depth

### Results and Discussions

The last column of the above table indicates the percentage of contribution (%P) of each factor, thus exhibiting the level of influence on the quality characteristics. The Table 4.3 shows tool diameter, steps size and feed rate have percentage contributions of 84.86, 9.09 and 3.04 on the final thickness of sheet blank respectively.

The last column of the Table 6 indicates the percentage contribution (% P) of each factor, thus exhibiting the level of influence on the quality characteristic. The Table 4.5 shows that the tool diameter, step size and feed rate had a percentage contributions of 0.63, 97.49 and 0.19% on the fracture depth of frustum of a cup respectively.

### CONCLUSION

From Taguchi analysis and ANOVA we can conclude that

- Vertical step size has a major influence on fracture depth
- Tool diameter influences the surface finish of the part
- In conventional forming sheet is under both simple tension and biaxial stretching
- In SPIF Wall surfaces are under Plane stretching condition and
- Corner surfaces are under biaxial stretching condition

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