

Multi-Manned Assembly Line Balancing using Genetic Algorithm

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Abstract - In this paper, the problem of balancing multi-manned assembly line (MAL) is tackled. Those lines are important for the assembly of medium and large sized products such as washers, air-conditioners, buses, trucks, helicopters....., etc. Nowadays, by the great improvement in the technology it is become possible to produce complex products with hundreds of tasks, this make a need to reduce line length for better space utilization. In this work a hybrid Genetic Algorithm (GA) is developed to solve multi-manned assembly line balancing problem. A new indicator (MPNW) is defined to determine the maximum permissible number of workers in the station. Number of stations expressing better utilization of the available area is considered as the performance criteria in this algorithm. To demonstrate the performance of the developed algorithm, it is tested on instances collected from the literature and it shows its effectiveness in solving this problem and gives a comparable results.

Keywords: *Multi-manned, assembly line balancing problem, genetic algorithm.*

1- INTRODUCTION

Assembly is the capstone process for product realization where component, parts, and subassemblies are integrated together to form the final products. Assembly line can be categorized into one-sided, two-sided, and multi-manned assembly lines.

One sided assembly line balancing problem is the problem of finding the best feasible solution of assigning tasks to stations. In one sided only one line is used with at most one worker in each station.

Two sided assembly line balancing problem consists of two serial lines in parallel instead of one line. Each station on the right and left side has at most one worker in which each worker do different works on the same work piece simultaneously

While multi-manned assembly line (MAL) balancing problems are a new type of generalized assembly line balancing problems in which there is the possibility of assigning more than one operator to each workstation according to the product features [1]. The differences between the two sided and multi manned are: 1) number of workers in each station and 2) in multi manned it is essential to assign the task to the worker after assigning it to the station as there is more than one worker in each

station. The maximum number of worker is determined by the designer according to certain criteria as the product size, tools availability, workstation designetc

The MAL is essential these days, especially in the assembly of large-sized products, as helicopter, buses and trucks. As the advance in technology and customer demand increases the complexity and number of tasks of product increases. This makes a need to a huge manufacturing plant in case of one sided assembly line. So the use of MAL becomes important especially in these cases. Up to day, factories have produced these types of products by allowing stations having multiple workers working in the same station and balancing the line by trial-and-error method [2].

Although multi manned assembly line is very common in real world, only small numbers of researchers focus on it. Dimitriadis [3] was the first one to introduce MAL problem, his proposed heuristic is a two-level procedure. The upper level generates all feasible assignable subsets of work elements to L workers working together on the same product and the same workstation, while the lower level proceeds to successfully allocate the work elements to each worker. The proposed approach results in shorter physical line length and production space utilization improvement, because the same number of workers can be allocated to fewer workstations.

Fattahi et al [1] proposed two approaches: (1) a mixed integer programming model for balancing the problem of assembly line with multi-manned workstations, and (2) an ant colony (ACO) meta-heuristic approach to efficiently solve the medium- and large-size scales of this problem. The model minimizes the total number of workers on the line as the first objective and the number of opened multi-manned workstations as the second one. The result showed that for a small sized problem, the mixed integer formulation can be used to obtain the optimal solution. However, as the size of the problem grows, the optimal solution may not be found in a reasonable amount of time. While for (ACO) experimental results show that it generates optimal solutions in small-size problems and outperforms the other approaches in terms of solution quality. Also, the proposed algorithm could reach the optimal number of workers on the line for all of the test problems (medium and large size).

Kellegoz et al [2] addressed assembly line balancing problem which has parallel multi-manned stations. A branch and bound algorithm called Jumper was developed,

to optimally solve the problem. Another branch and bound algorithm in the literature was modified to solve it and compared with Jumper. Through an analysis of the results, it is seen that Jumper showed better performance than does the latter one. However, the algorithm's performance was questionable to solve big-size assembly line balancing problems.

Roshani et al [4] developed simulated annealing algorithm (SA) for MALB problem in order to maximize the line efficiency, minimize the line length and minimize the smoothness index. The proposed SA algorithm is compared with the ACO in minimizing the number of workstations showed that the proposed SA algorithm is effective than ACO in minimizing the number of multi-manned workstations.

Kazemi et al [5] used a cost-oriented approach to model the MALBP with the aim of minimizing total cost per production unit. Genetic algorithm was used to solve medium and large sized problem. The results showed that the GA performs significantly better than other algorithms and for all examples the average required space has reduced to 45.95 percent of its previous value for the traditional approach.

From the previous survey it can be found that, although MAL is important these days only few researchers focus on it. According to literature most researchers consider determining the maximum permissible number of workers per station is the duty of the designer. Kazemi et al [5] states that GA performs significantly better than other algorithms. For this reason a hybrid genetic algorithm is proposed to solve a multi-manned assembly line balancing problem. The model aims to minimize the length of the line and improve the space utilization with minimum number of workers. A heuristic is proposed to assign tasks to stations and workers. A new indicator called MPNW (maximum permissible number of worker) is defined to determine the maximum number of workers permitted per station.

The rest of this paper is organized as follows: Section 2 presents description of MAL balancing problem. In section 3, the proposed indicator MPNW is defined, the developed genetic algorithm is explained in section 4. Section 5 concludes the main results, and finally section 6 is the conclusion and future work.

2- DESCRIPTION OF MULTI MANNED ASSEMBLY LINE BALANCING PROBLEM.

As mentioned before the main characteristic of MAL is that more than one worker can be assigned to each station. Each worker performs different work simultaneously on the same product. The number of worker in each station can be different from one station to other as seen in fig

The basic characteristic of MAL can be stated as follows [2]:

1. More than one worker can perform different tasks simultaneously on the same product
2. Each worker can perform only one task at a time
3. Precedence constraint should not be violated when assigning tasks to workers

4. Number of workers can be different from one station to another
5. Maximum number of workers in any station cannot exceed the maximal permitted number of workers

The main advantage of MAL over simple assembly line [3]:

1. It can shorten the line length, i.e. space utilization improvement
2. It reduce the amount of throughput time and work in process (WIP)
3. It can lower material handling costs, since it reduces the need for workers to maneuver tools, parts, or the product.
4. There might be time and tool savings since workers working together in the same multi-manned workstation can share tools or fixtures

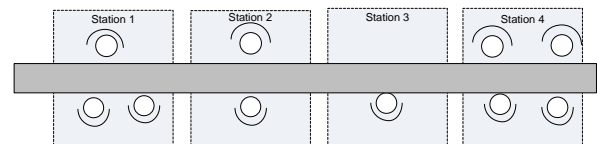


Figure 1 Multi manned assembly line

3- THE PROPOSED INDICATOR MPNW

According to Sanders et al [6] the recommended working area for the human hand is shown in Figure 2. The normal distance is 120 cm while the maximum distance is 150 cm. For the workers in the same station to not interfere with each other or block the movement of each other, each worker need at least distance equal to the max distance to work in. If we consider the max distance as the distance in which the worker can work freely. Then the MPNW will be as follows:

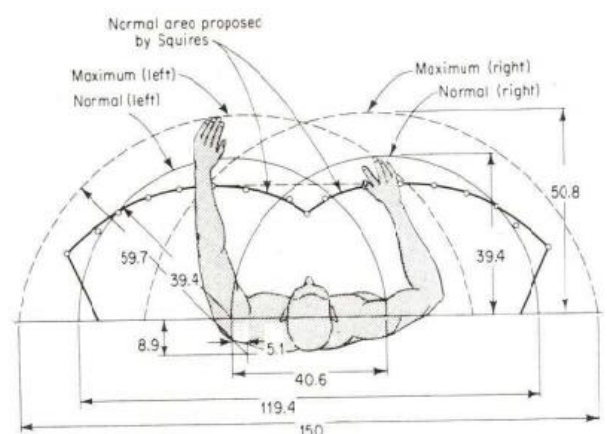


Figure 2 : Recommended working area for the hand of human-bien (Sanders and McCormick, 1993)

- a- If all tasks are assembled on one side of the product

$$MPNW = \frac{\text{length of this side}}{150 \text{ (cm)}} \quad (1)$$

- b- If tasks are assembled on both sides only of the products

$$MPNW = \frac{\text{sum of length of both sides}}{150 \text{ (cm)}} \quad (2)$$

- c- If tasks are assembled all round of the product

$$MPNW = \frac{\text{perimeter of the product}}{150 \text{ (cm)}} \quad (3)$$

This indicator is applied for the assembly of products that require the operator to be fixed in his place and the components are reachable to his hand as electronics products (television, computers...etc)

4- The proposed model

Nomenclature :	
β	: Controlling parameter to give flexibility to the solution by changing UB
T	: Number of tasks , $I = \{1, \dots, T\}$
W	: Number of workers, $W = \{1, \dots, K\}$
CT	: Cycle time
NS	: Number of stations
IDT	: Idle time
TNS	: Total number of all stations
TNW	: Total Number of workers in all stations
P_s	: Population size
t_i	: Time of task t
P_{ij}	: Precedence matrix , where $P_{ij} = \begin{cases} 1 & \text{if task } i \text{ precedes task } j \\ 0 & \text{otherwise} \end{cases}$
W_{LB}	: Worker lower bound
W_{max}	: Maximum number of workers per mated station
W_{min}	: Minimum number of workers per mated station
$D_{tsr/l}$: Delay time of station S at right or left side
W_{ws}	: Worker number W in station S
S_{ATSW}	: Set of assigned tasks T to station S to worker W
IT_s	: Ideal time per station
Sc_g	: Sequence of task come from genetic after mutation and crossover
NW_s	: Number of worker per station S
Sc_{UA}	: Set of candidate of unassigned tasks
TWL_{ws}	: Total work load of worker W in station S

Initial population (encoding stage)

In the proposed model the genetic algorithm is used to sequence the tasks into feasible order. Task based representation scheme of the chromosomes is used. Each gene in the chromosome represents the task number. Beside the random generation of the initial population six well known heuristic is added. This six well-known heuristics are : (Baykasoglu [7]) maximum ranked positional weight, largest candidate rule, maximum number of followers, min slack value, the minimum early start, and maximum processing time divided by the upper bound of task t.

Decoding stage:

In this stage each chromosome from the encoding stage is assigned to stations according to the following heuristic:

Step 1:

Enter Input data: Cycle time (ct), Precedence matrix (P_{ij}), Task time (t_i), Max number of workers per mated station (W_{max}), Min number of worker per station (W_{min}), Controlling parameter β

Step 2:

- Calculate the lower bound of worker (W_{LB})

$$W_{LB} = \text{Round} \left(\frac{\sum_{i=1}^N t_i}{ct} \right) \quad (4)$$

- Calculate upper bound of idle time (UB)

$$UB = \beta * \frac{ct * W_{LB} - \sum_{i=1}^N t_i}{W_{LB}} \quad (5)$$

- Number of station (NS)=1

Step 3:

From Sc_g start with the first element until $Sc_g = \{\emptyset\}$; if $Sc_g = \{\emptyset\}$ go to step 7

Step 4:

- Assign task t to its side to the worker which it's $TWL_{ws} + t_i \& FTP_{ws} + t_i \leq ct$ if task t can't be assigned to any worker go to step 6
- If more than worker fulfill this condition assign the task to the worker that has min delay time (D_t)

D_t = start time of task t – end time of task j

- If more than worker has equal D_t choose the worker that will start it first (worker with min TWL)
- If more than worker has min TWL choose worker randomly
- Update P_{ij}

Step 5:

Calculate average idle time per station (IT_s)

$$IT_s = \frac{ct \cdot W_s - \sum_{i \in S} t_i}{W_s} \quad (6)$$

If $IT_s > UB$ and $W_s > W_{min}$ cancel one worker at a time and rebalance the problem until IT_s

Step 6:

Open new station with $NS = NS + 1$ then go to step 3

Step 7:

End

Fitness function

After decoding stage, each chromosome is evaluated using fitness function, according to the fitness value, the chromosome is selected for the next generation or replaced. The fitness function is derived from the objective function and used in successive genetic operation. The developed GA employs the functions given in Eq (6, and 7) as the fitness function. This function evaluates the number of workers and thenumber of stations.

- *Minimize F*. $F(1) = \sum_{g=1}^{NS} \sum_{w=1}^K NW_{wS}$ (7)

- *Minimize F*. $F(2) = NS$ (8)

Genetic algorithm operators

In the proposed model the reminder selection of Matlab @, two point cross over technique proposed by Leu et al. [8], and scramble mutation are used as genetic operators. Values are listed in Table 1.

Table 1 Parameters of genetic operators

Parameter	problems
Population size (Ps)	20
Crossover rate (Rc)	0.8
Mutation rate (Rm)	0.2
Elite (e)	2

Stopping criteria

Several stopping conditions can be applied for the GA. In the developed GA the stopping condition is reaching a determined number of generations as given in Table 1.

5- RESULTS

In order to examine the performance of the proposed model, the proposed algorithm was applied to solve 62 instances collected from Talbot et al [9] known as Talbot data set. Five small size problems, proposed by Merten [10], Bowman [11], Jaeschke [12], Jackson [13], and Mansoor [14], four medium size, presented by Mitchell [15], Heskia [16], Sawyer [17], Kilbridge and Wester [18], and three large-sized problems, presented by Tonge [19] and Arcus [20]. Table 2 shows the comparison of the results of the proposed algorithm with similar studies from the literature. This studies are: Group forming method (GM) which proposed by Dimitriadis [3]. Ant colony optimization (ACO) is proposed by Fattahi et al [1], and Roshani et al [4] used simulated annealing. Two solution evaluation criteria are considered which are: the numbers of stations (NS), and the number of workers (NW)

From Table 2 it can be seen that the proposed algorithm is capable of balancing efficiently the multi-manned assembly line balancing problem. The proposed model could find optimum solution in 60 instances out of 62. The results show also the advantage of MAL balancing problem over SALBP as it saves from 25 % to 50 % of the line length, which means better utilization of the available area, lower cost of fixtures and less workers movement. The proposed model gives better space saving than the similar studies from the literature in 10 instances. This proves the effectiveness of adding well-known heuristic to the random run of the initial population.

6- CONCLUSION

In this paper multi-manned assembly line balancing problem (MALPB) is addressed in order to minimize the line length and the number of workers. Although MAL is essential as it make better usage of the available area especially for large products as cars, trucks and helicopter only few literatures was concerned with it.

A new indicator called MPNW is defined. It determines the maximum permissible number of workers per station. The designers can use it to state if the product can overloaded more than one worker or not and how many workers can be assigned to it.

The developed GA is compared to the similar studies in the literature and it is found that the proposed algorithm could find optimum solution (lower bound of number of workers) in 97 % of the all test problems under consideration. This prove the effectiveness of the proposed hybrid genetic algorithm and the proposed heuristic in solving the problem of MALPB.

The results emphasis the advantage of MAL over simple assembly line, as it saves from 25 to 50% of the total line length, this means better utilization of the available area, lower cost of fixtures and less workers movement.

Table 2 Comparison of the result with the bench mark problem

Author	CT	LB (NW)	GM		ACO		SA		Prop.GA		
			NW	NS	NW	NS	NW	NS	NW	NS	% area saving
Merten (7)	6	6	6	6	6	3	6	3	6	3	50
	7	5	5	5	5	3	5	3	5	3	40
	8	5	5	5	5	3	5	3	5	3	40
	10	3	3	3	3	3	3	3	4	3	0
	15	2	2	2	2	2	2	2	2	2	50
	18	2	2	2	2	2	1	2	1	2	1
Bowman(8)	17	5	-	-	5	5	5	5	5	5	0
	20	5	5	5	-	-	5	4	5	4	20
	21	5	-	-	5	4	5	4	5	4	0
	24	4	-	-	4	4	4	4	4	4	0
	28	3	-	-	3	2	3	2	3	2	33
	31	3	-	-	3	2	3	2	3	2	33
Jaeschke(9)	6	8	8	8	8	6	8	6	8	5	38
	7	7	7	7	7	6	7	6	7	5	29
	8	6	6	6	6	5	6	5	6	5	17
	10	4	4	4	4	4	4	4	4	4	0
	18	3	3	3	3	2	3	2	3	2	33
Jackson(11)	7	8	8	7	8	6	8	6	9	5	38
									8	6	33
	9	6	6	5	6	4	6	4	6	4	20
	10	5	6	6	5	4	5	4	5	4	25
	13	4	4	4	4	3	4	3	4	3	25
	14	4	4	4	4	3	4	3	4	3	33
	21	3	3	3	3	2	3	2	3	2	
Mansor(11)	45	5	-	-	5	3	5	3	5	3	40
	54	4	-	-	4	3	4	3	4	3	25
	63	3	-	-	3	2	3	2	3	2	33
	72	3	-	-	3	2	3	2	3	2	33
	81	3	-	-	3	2	3	2	3	2	33
Mitchell(21)	14	8	9	9	8	7	8	7	8	7	13
	15	8	8	8	8	7	8	7	8	7	13
	21	5	5	5	5	5	5	5	6	4	20
									5	5	0
	26	5	5	5	5	4	5	4	5	4	20
	35	3	3	3	3	3	3	3	3	3	50
	39	3	3	3	3	2	3	2	3	2	33
Heskia(28)	138	8	8	6	8	5	8	5	8	4	50
	205	5	6	6	5	3	5	3	5	3	40
	216	5	5	4	5	3	5	3	5	3	40
	256	4	5	5	4	3	4	3	4	3	25
	324	4	4	3	4	2	4	2	4	2	50
	342	3	3	3	3	2	3	2	3	2	33
Kilbridge(45)	57	10	10	8	10	6	10	6	10	5	50
	79	7	7	6	7	5	7	5	8	4	43
									7	5	29
	92	6	6	5	6	4	6	4	7	4	33
	110	6	6	5	6	3	6	3	6	3	50
	138	4	4	4	4	3	4	3	4	3	25
	184	3	3	3	3	2	3	2	3	2	33
Tonge(70)	176	21	22	21	21	20	21	19	21	14	33
	364	10	10	9	10	7	10	7	10	5	50
	410	9	9	7	9	6	9	5	9	4	56
	468	8	8	7	8	4	8	4	8	4	50
	527	7	7	7	7	4	7	4	7	4	43

Arcus(83)	5048	16	16	16	16	11	16	11	16	11	31
	5853	14	14	13	14	10	14	9	14	10	29
	6842	12	12	10	12	8	12	8	12	8	33
	7571	11	11	11	11	7	11	7	11	7	36
	8412	10	10	10	10	6	10	6	10	6	40
	8998	9	9	8	9	6	9	6	9	6	33
	10816	8	8	8	8	5	8	5	8	6	25
Arcus(111)	5755	27	27	24	27	20	27	21	27	14	48
	8847	18	18	18	18	12	18	12	18	12	33
	10027	16	16	15	16	10	16	11	16	10	38
	10743	15	15	14	15	10	15	10	15	10	33
	11378	14	14	9	14	9	14	9	14	7	50
	17067	9	9	7	9	6	9	6	9	5	44

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